Please check the examination details below before entering your candidate information			
Candidate surname  mel@jvstmath	o.cock Other names		
Pearson Edexcel International GCSE	Centre Number	Candidate Number	
Thursday 7 January 2021			
Morning (Time: 2 hours)	Paper Reference <b>4</b>	MA1/1H	
<b>Mathematics</b>	A		
Paper 1H Higher Tier	WORKED SOLUTIONS		
You must have: Ruler graduated in centimetres a pen, HB pencil, eraser, calculator	and millimetres, protractor, compa . Tracing paper may be used.	Total Marks	

## **Instructions**

- Use **black** ink or ball-point pen.
- Fill in the boxes at the top of this page with your name, centre number and candidate number.
- Answer all questions.
- Without sufficient working, correct answers may be awarded no marks.
- Answer the questions in the spaces provided
  - there may be more space than you need.
- Calculators may be used.
- You must **NOT** write anything on the formulae page. Anything you write on the formulae page will gain NO credit.

#### Information

- The total mark for this paper is 100.
- The marks for **each** question are shown in brackets
  - use this as a guide as to how much time to spend on each question.

#### **Advice**

- Read each question carefully before you start to answer it.
- Check your answers if you have time at the end.

Turn over ▶





## **International GCSE Mathematics**

## Formulae sheet - Higher Tier

#### **Arithmetic series**

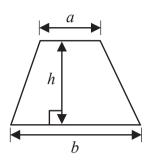
Sum to *n* terms,  $S_n = \frac{n}{2} [2a + (n-1)d]$ 

## The quadratic equation

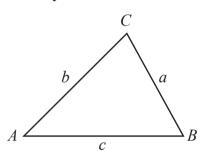
The solutions of  $ax^2 + bx + c = 0$  where  $a \neq 0$  are given by:

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Area of trapezium =  $\frac{1}{2}(a+b)h$ 



## **Trigonometry**



In any triangle ABC

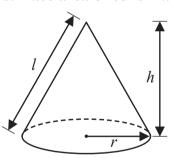
Sine Rule 
$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

Cosine Rule 
$$a^2 = b^2 + c^2 - 2bc \cos A$$

Area of triangle = 
$$\frac{1}{2}ab\sin C$$

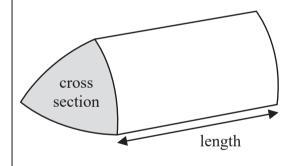
# **Volume of cone** = $\frac{1}{3}\pi r^2 h$

Curved surface area of cone =  $\pi rl$ 

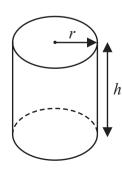


## Volume of prism

= area of cross section  $\times$  length

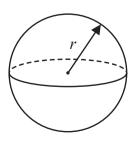


## Volume of cylinder = $\pi r^2 h$ Curved surface area of cylinder = $2\pi rh$



Volume of sphere = 
$$\frac{4}{3}\pi r^3$$

Surface area of sphere =  $4\pi r^2$ 



## **Answer ALL TWENTY FOUR questions.**

## Write your answers in the spaces provided.

## You must write down all the stages in your working.

Pieter owns a currency conversion shop.

Last Monday, Pieter changed a total of 20160 rand into a number of different currencies.

He changed  $\frac{3}{10}$  of the 20 160 rand into euros.

He changed the rest of the rands into dollars, rupees and francs in the ratios 9:5:2

Pieter changed more rands into dollars than he changed into francs.

Work out how many more.

20160 rand

the rest = 20160-6048

Dollas: rupees: francs 9 5 2

14112 : 16 = 882

7938 4410

Jerence => 7938-1764

(Total for Question 1 is 4 marks)

2 The table gives information about the speeds, in kilometres per hour, of 80 motorbikes as each pass under a bridge.

Speed (s kilometres per hour)	Frequency
$40 < s \le 50$	10
$50 < s \le 60$	16
$60 < s \leqslant 70$	19
$70 < s \leqslant 80$	23
$80 < s \le 90$	12
	CVM

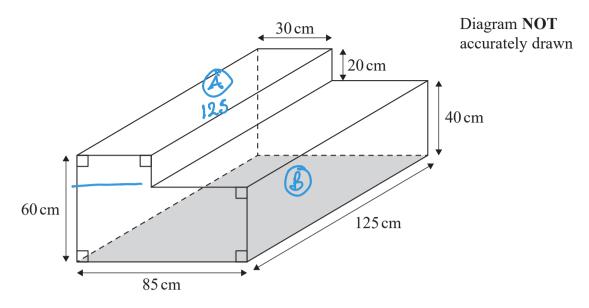
(a) Write down the modal class.

(b) Work out an estimate for the mean speed of the motorbikes as they pass under the bridge. Give your answer correct to 3 significant figures.

kilometres per hour

(Total for Question 2 is 5 marks)

3 The diagram shows a container for water in the shape of a prism.



The rectangular base of the prism, shown shaded in the diagram, is horizontal. The container is completely full of water.

Tuah is going to use a pump to empty the water from the container so that the volume of water in the container decreases at a constant rate.

The pump starts to empty water from the container at 1030 and at 1200 the water level in the container has dropped by 20 cm.

Find the time at which all the water has been pumped out of the container.

$$V_{OLA} = 30 \times 20 \times 125$$
  $V_{OLB} = 85 \times 40 \times 125$   
= 75000cm<sup>3</sup> = 425000 cm<sup>3</sup>

A emphes in Thow 30 mins so rate of flow = 
$$\frac{75000}{90}$$
 =  $\frac{733.3 \text{ cm}^3/\text{min}}{30}$ 

20:30

(Total for Question 3 is 4 marks)



**4**  $\mathscr{E}$ = {20, 21, 22, 23, 24, 25, 26, 27, 28, 29}

$$A = \{ \text{odd numbers} \}$$
 2: 23 25 27 29  $B = \{ \text{multiples of } 3 \}$  2: 24

List the members of the set

(i) 
$$A \cap B$$

(ii)  $A \cup B$ 

(Total for Question 4 is 2 marks)

5 (a) Factorise fully  $15y^4 + 20uy^3$ 

(b) Solve 
$$4 - 3x = \frac{5 - 8x}{4}$$

Show clear algebraic working.

$$4(4-30c) = 5-80c$$
 $16-120c = 5-80c$ 
 $16-5 = -80c+120c$ 
 $11 = 40c$ 
 $0c = \frac{11}{4}$ 

$$x = \frac{2 \cdot 75}{(3)}$$

## (Total for Question 5 is 5 marks)

**6** (a) Write 2 840 000 000 in standard form.

(b) Write  $2.5 \times 10^{-4}$  as an ordinary number.



(Total for Question 6 is 2 marks)



7 Chen invests 40 000 yuan in a fixed-term bond for 3 years.

The fixed-term bond pays compound interest at a rate of 3.5% each year.

(a) Work out the value of Chen's investment at the end of 3 years. Give your answer to the nearest yuan.

Wang invested *P* yuan.

The value of his investment decreased by 6.5% each year.

At the end of the first year, the value of Wang's investment was 30481 yuan.

(b) Work out the value of P.

100 - 6.5 : 93.5

$$P = \frac{32600}{(3)}$$

(Total for Question 7 is 6 marks)



**8** The region, shown shaded in the diagram, is a path.

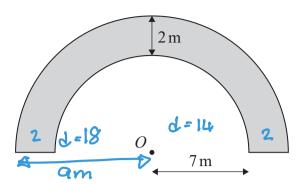


Diagram **NOT** accurately drawn

The boundary of the path is formed by two semicircles, with the same centre *O*, and two straight lines.

The inner semicircle has a radius of 7 metres. The path has a width of 2 metres.

Work out the perimeter of the path. Give your answer correct to one decimal place.

$$\frac{1}{2}\pi x^{18} + \frac{1}{2}\pi x^{14} + 2 + 2$$

$$= 54 \cdot 2654 \dots$$

$$\uparrow$$
(1dp)

54.3

n

(Total for Question 8 is 3 marks)



**9** (a) Simplify  $(2x^3y^5)^4$ 

162012 y 20

(b) (i) Factorise 
$$x^2 + 5x - 36$$

$$(x+9)(x-4)$$

(ii) Hence, solve 
$$x^2 + 5x - 36 = 0$$

$$(2c + 9)(2c - 4) = 0$$
 $\frac{1}{4}$ 
 $\frac{1}{4}$ 

(Total for Question 9 is 5 marks)

**10** Here is isosceles triangle *ABC*.

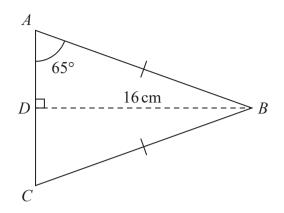
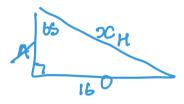


Diagram NOT accurately drawn

D is the midpoint of AC and  $DB = 16 \,\mathrm{cm}$ .

Angle  $DAB = 65^{\circ}$ 

Work out the perimeter of triangle ABC. Give your answer correct to one decimal place.

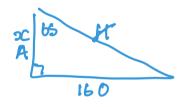


$$sin 65 = 16$$

$$8 \times 65 = 16$$

$$\approx 20 = 16$$

$$\approx 17.65 \times ...$$



$$tan bS = \frac{1b}{2c} \qquad bc = \frac{1b}{tan bS}$$

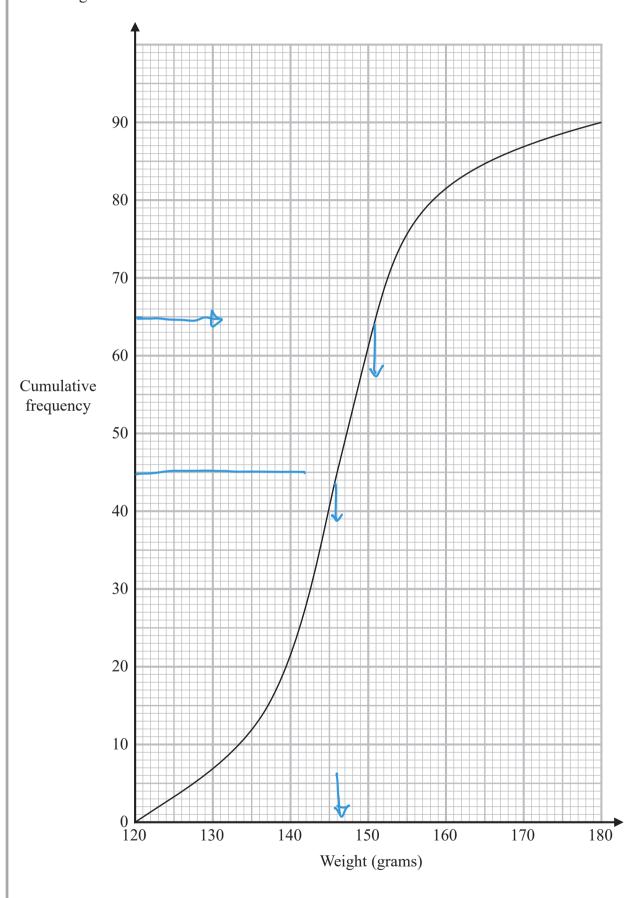
$$banbS$$

$$= 7.4669...$$

50:2 cm

(Total for Question 10 is 4 marks)

11 The cumulative frequency graph gives information about the weights, in grams, of 90 bags of sweets.



(a) Find an estimate for the median of the weights of these bags of sweets.

Roberto sells the bags of sweets to raise money for charity. Bags with a weight greater than d grams are labelled large bags and sold for 3.75 euros each bag.

The total amount of money he receives by selling all the large bags is 93.75 euros.

(b) Find the value of d.

$$d = \frac{151}{(3)}$$

(Total for Question 11 is 5 marks)

12 (a) Express  $\frac{4}{x-2} - \frac{3}{x+1}$  as a single fraction.

Give your answer in its simplest form.

$$4(x+1) - 3(x-2)$$

$$(x-2)(x+1)$$

$$= 4x + 4 - 3x + 6$$

$$(x - 2)(x + 1)$$

= 
$$2c + 10$$
  
(2c -2)(2c +1)

$$\frac{x+10}{(x-2)(x+1)}$$

(b) Expand and simplify 2x(x-5)(x-3)

$$= 2x(x^2-8x+15)$$

$$= 2x^3 - 16x^2 + 30x$$

$$2x^3 - 16x^2 + 30x$$

(Total for Question 12 is 6 marks)

- **13** Point *A* has coordinates (5, 8) Point *B* has coordinates (9, –4)
  - (a) Work out the gradient of AB.

gradient = 
$$\frac{-4-8}{9-5}$$
  
=  $-\frac{12}{4}$  =  $-3$ 

**-3** (2)

The straight line L has equation y = -4x + 5

(b) Write down the gradient of a straight line that is perpendicular to L.

$$m_1 m_2 = -1$$

$$-4 \times m_2 = -1$$

$$m_2 = -\frac{1}{-4} = \frac{1}{4}$$

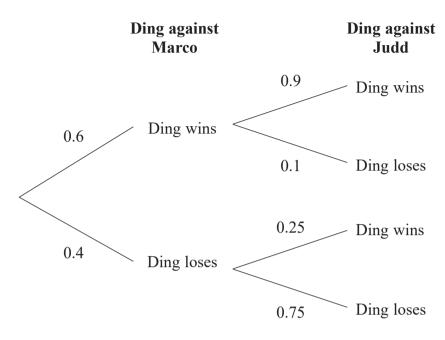
14

(1)

(Total for Question 13 is 3 marks)

14 Ding is going to play one game of snooker against each of two of his friends, Marco and Judd.

The probability tree diagram gives information about the probabilities that Ding will win or lose each of these two games.



(a) Work out the probability that Ding will win both games.

O·54

(b) Work out the probability that Ding will win exactly one of the games.

O·16

(Total for Question 14 is 5 marks)

$$a = \frac{v - u}{t}$$

v = 9.6 correct to 1 decimal place

u = 3.8 correct to 1 decimal place

t = 1.84 correct to 2 decimal places

Calculate the upper bound for the value of a.

Give your answer as a decimal correct to 2 decimal places.

Show your working clearly.

$$v = 9.6$$
 $v = 9.6$ 
 $v =$ 

3.25

(Total for Question 15 is 3 marks)

**16** The diagram shows the positions of three ships, A, B and C.

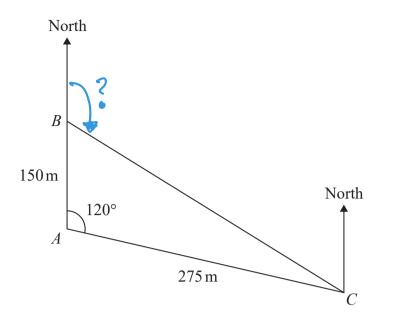


Diagram **NOT** accurately drawn

Ship B is due north of ship A.

The bearing of ship C from ship A is  $120^{\circ}$ 

Calculate the bearing of ship *C* from ship *B*.

Give your answer correct to the nearest degree.

$$BC^2 = 150^2 + 275^2 - 2 \times 150 \times 275 \times cos 120$$
  
= 139 375  
 $BC = \sqrt{139375} = 25\sqrt{223}$ 

angle 
$$\widehat{ABC}$$

$$\frac{SINB}{27S} = \frac{SIN120}{25\sqrt{223}}$$

$$B = SIN^{-1} \left[ \frac{SIN120}{25\sqrt{223}} \times 275 \right]$$



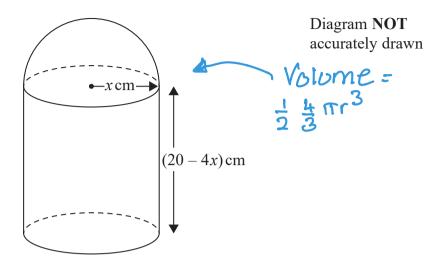
= 39.637..

140

(Total for Question 16 is 5 marks)

## 17 A solid, S, is made from a hemisphere and a cylinder.

The centre of the circular face of the hemisphere and the centre of the top face of the cylinder are at the same point.



The radius of the cylinder and the radius of the hemisphere are both x cm. The height of the cylinder is (20 - 4x) cm.

The volume of **S** is  $V \text{ cm}^3$  where  $V = \frac{1}{3} \pi y$ 

Find the maximum value of *y*. Show clear algebraic working.

$$V = \frac{1}{2} \times \frac{1}{3} \operatorname{TDC}^{3} + \operatorname{TDC}^{2} \times (20 - 4 \times 2)$$

$$= \frac{4}{6} \operatorname{TDC}^{3} + 20 \operatorname{TDC}^{2} - 4 \operatorname{TDC}^{3}$$

$$= (\frac{2}{3} \times -4 \times) \times^{3} + 20 \times \times^{2} = \frac{1}{3} \operatorname{PY}$$

$$(3) = (2 - 12) \times^{3} + 60 \times^{2} = 9$$

$$\therefore y = 60 \times^{2} - 10 \times^{3}$$

$$\frac{dy}{dx} = 120x - 30x^{2}$$

$$120x - 30x^{2} = 0$$

$$30x^{2} = 120x$$

$$x = \frac{120}{30} = 4$$

$$y = 60x 4^{2} - 10x 4^{3}$$

$$= 320$$

320

## (Total for Question 17 is 5 marks)

18 Given that  $(8 - \sqrt{x})(5 + \sqrt{x}) = y\sqrt{x} + 21$  where x is a prime number and y is an integer, find the value of x and the value of y. Show each stage of your working clearly.

 $x = \frac{19}{y}$   $y = \frac{3}{2}$ 

(Total for Question 18 is 3 marks)



19 Solve the simultaneous equations

$$x^{2} - 9y - x = 2y^{2} - 12$$
$$x + 2y - 1 = 0$$

Show clear algebraic working.

$$1 - 4y + 4y^{2} - 9y - (1-2y) = 2y^{2} - 12$$

$$1 - 4y + 4y^{2} - 9y - 1 + 2y - 2y^{2} + 12 = 0$$

$$2y^{2} - 11y + 12 = 0$$

$$(2y - 3)(y - 4) = 0$$

$$y = \frac{3}{2} \qquad y = 4$$

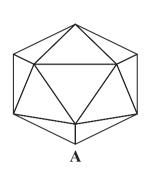
$$x = 1 - 2(\frac{3}{2}) \qquad y = 1 - 2 \times 4$$

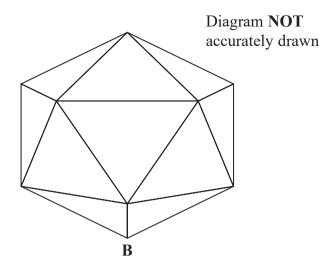
$$= -7$$

$$x = -2$$
  $x = -\frac{1}{2}$   $y = 4$ 

(Total for Question 19 is 5 marks)

**20** A and B are two similar solids.





A has a volume of 1836 cm<sup>3</sup>

**B** has a volume of 4352 cm<sup>3</sup>

**B** has a total surface area of 1120 cm<sup>2</sup>

Work out the total surface area of A.

length 
$$8F = 3 \int \frac{63}{27} = \frac{4}{3}$$
area  $8F = \left(\frac{4}{3}\right)^2 = \frac{16}{9}$ 

area SF = 
$$(\frac{4}{3})^2 = \frac{16}{9}$$

5. Area of 
$$A = 1120 \div \frac{16}{9}$$

630 cm<sup>2</sup>

(Total for Question 20 is 3 marks)

## **21** A curve has equation y = f(x)

The coordinates of the minimum point on this curve are (-9, 15)

(a) Write down the coordinates of the minimum point on the curve with equation

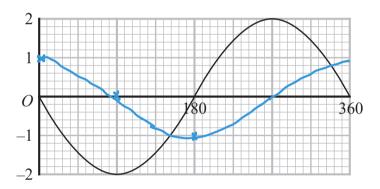
(i) 
$$y = f(x + 3)$$

(-12, 5)

(ii) 
$$y = \frac{1}{3} f(x)$$



The graph of  $y = a\cos(x+b)^{\circ}$  for  $0 \le x \le 360$  is drawn on the grid below.



Given that a > 0 and that 0 < b < 360

(b) find the value of a and the value of b.

$$a = \frac{2}{b}$$

$$b = \frac{2}{(2)}$$

(Total for Question 21 is 4 marks)



22 The function f is such that  $f(x) = x^2 - 8x + 5$  where  $x \le 4$ 

Express the inverse function  $f^{-1}$  in the form  $f^{-1}(x) = ...$ 

$$y = (x - 4)^{2} - 16 + 5$$

$$= (x - 4)^{2} - 11$$

$$y + 11 = (x - 4)^{2}$$

$$y + 11 = x - 4$$

$$x = 4 + y + 1 guen x \le 4$$

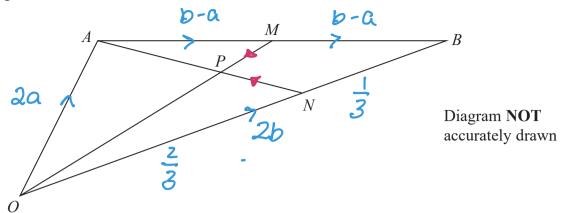
$$x = 4 - y + 1$$

:. 
$$f^{-1}(x) = 4 - \sqrt{x+1}$$

$$f^{-1}(x) = 4 - \sqrt{2c + 1}$$

(Total for Question 22 is 3 marks)

## **23** *OAB* is a triangle.



$$\overrightarrow{OA} = 2\mathbf{a}$$
 and  $\overrightarrow{OB} = 2\mathbf{b}$ 

M is the midpoint of AB.

N is the point on OB such that ON: NB = 2:1

$$= 2a + \lambda \left(\frac{4}{3}b - 2a\right)$$

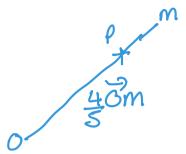
P is the point on AN such that OPM is a straight line.

Use a vector method to find *OP*: *PM* Show your working clearly.

$$\vec{O} \rho = \mu(a+b)$$

$$\vec{op} = \frac{4}{3}b + 7(-\frac{4}{3}b + 2a)$$

x3



4:1

(Total for Question 23 is 6 marks)

**Turn over for Question 24** 

**24** An arithmetic series has first term *a* and common difference *d*.

The sum of the first 2n terms of the series is four times the sum of the first n terms of the series.

Find an expression for a in terms of d. Show your working clearly.

$$S_{2n} = \frac{\partial n}{\partial t} (2a + (2n-1)d)$$

$$= n(2a + 2nd - d)$$

$$= 2na + 2n^2d - nd$$

$$= na + \frac{n^2d}{2} - \frac{nd}{2}$$

$$2na + 2n^{2}d - nd = 4(na + n^{2}d - nd)$$

$$2na + 2n^{2}d - nd = 4na + 2n^{2}d - 2nd$$

$$0 = 4na - 2na - 2nd + nd$$

$$= 2na - nd$$

$$d = 2a$$

$$a = \frac{d}{2}$$

(Total for Question 24 is 4 marks)

TOTAL FOR PAPER IS 100 MARKS